

**PRE-CALCULUS:** by Finney, Demana, Watts and Kennedy  
Sums of Powers of Integers

$$3 + 1 + (-4) + (-1)$$

$$\frac{n(n+1)(2n+1)}{6}$$

$$\frac{4(4+1)(2(4)+1)}{6}$$

$$\frac{4(5)(9)}{6}$$

Find the sum

$$A) \sum_{n=1}^4 2 + \frac{5}{2}n - \frac{3}{2}n^2 = -12 \quad a_1 = 2 + \frac{5}{2}(1) - \frac{3}{2}(1)^2 \\ \frac{4}{2} + \frac{5}{2} - \frac{3}{2} = \frac{6}{2} = 3$$

$$a_4 = 2 + \frac{5}{2}(4) - \frac{3}{2}(4)^2$$

$$2 + 10 - 24$$

$$a_2 = 2 + \frac{5}{2}(2) - \frac{3}{2}(2)^2$$

$$2 + 5 - 6$$

$$a_3 = 2 + \frac{5}{2}(3) - \frac{3}{2}(3)^2$$

$$\frac{4}{2} + \frac{15}{2} - \frac{27}{2} = \frac{-8}{2} = -4$$

$$B) \sum_{n=1}^5 n^2 + 5 = 80$$

$$a_1 = 1^2 + 5 = 6$$

$$a_5 = 5^2 + 5 = 30$$

$$a_2 = 2^2 + 5 = 9$$

$$6 + 9 + 14 + 21 + 30$$

$$a_3 = 3^2 + 5 = 14$$

$$a_4 = 4^2 + 5 = 21$$

$$C) \sum_{n=1}^6 n^3 =$$

$$441$$

$$a_1 = 1 \quad a_4 = 64$$

$$a_2 = 8 \quad a_5 = 125$$

$$a_3 = 27 \quad a_6 = 216$$

Find the sum

A)  $\sum_{n=1}^{15} 2 + \frac{5}{2}n - \frac{3}{2}n^2 =$

B)  $\sum_{n=1}^{20} n^2 + 5 =$

C)  $\sum_{n=1}^{20} n^3 =$

List the formulas for the following sums of powers of integers.

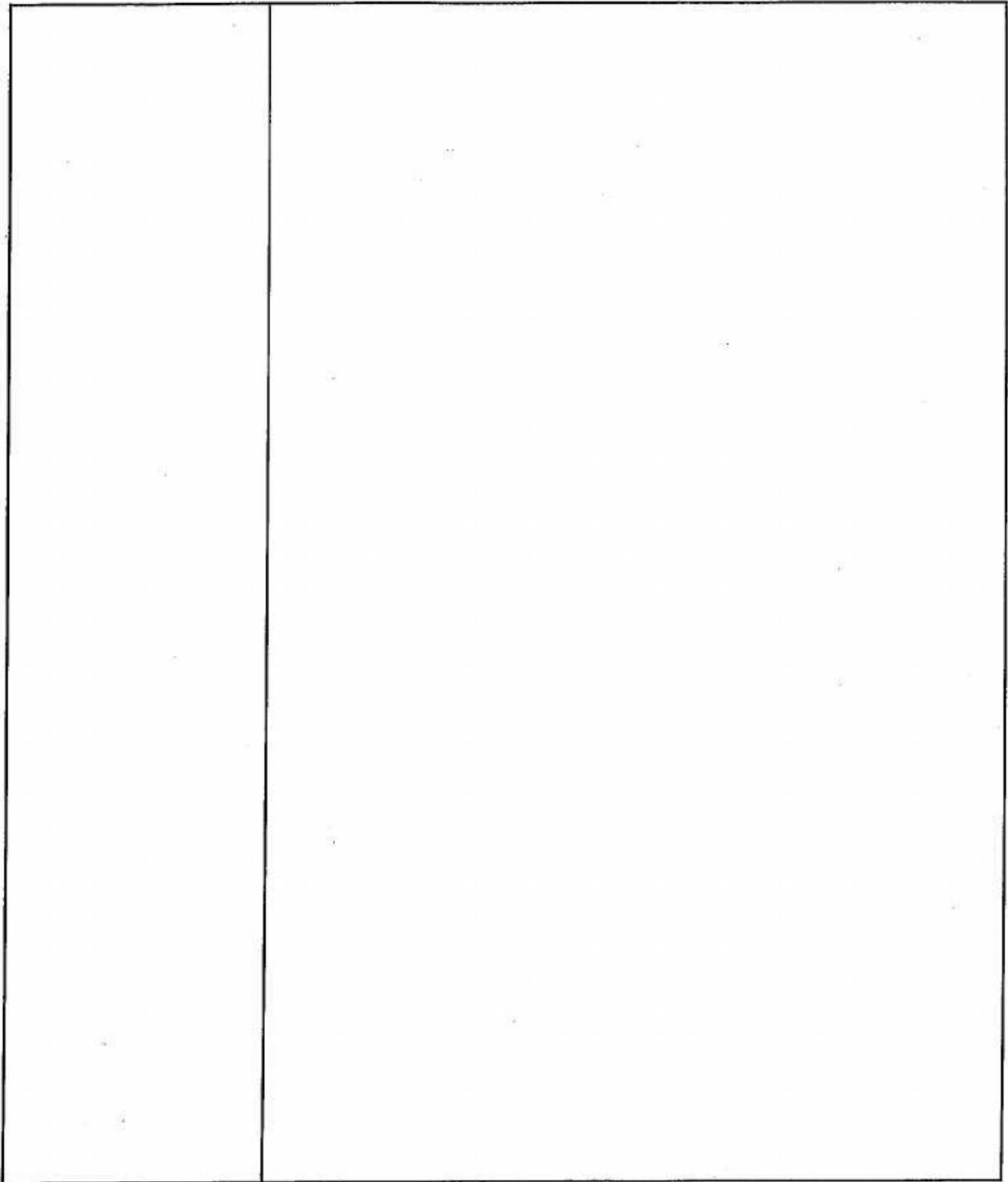
1.  $1 + 2 + 3 + 4 + \dots + n = \underline{n(n+1)/2}$

2.  $1^2 + 2^2 + 3^2 + 4^2 + \dots + n^2 = \underline{n(n+1)(2n+1)/6}$

3.  $1^3 + 2^3 + 3^3 + 4^3 + \dots + n^3 = \underline{n^2(n+1)^2/4}$

4.  $1^4 + 2^4 + 3^4 + 4^4 + \dots + n^4 = \underline{n(n+1)(2n+1)(3n^2+3n-1)/30}$

5.  $1^5 + 2^5 + 3^5 + 4^5 + \dots + n^5 = \underline{n^2(n+1)^2(2n^2+2n-1)/12}$



**PRE-CALCULUS:** by Finney, Demana, Waits and Kennedy  
 Limits of a Sequence

Find the limit of the sequence

A)  $a_n = \frac{3n+1}{2n}$

$a_1 = 2$      $a_5 = 1.6$      $a_9 = 1.5$

$\lim_{x \rightarrow \infty} =$

$a_2 = 1.75$      $a_4 = 1.583$      $a_{10} = 1.55$

$a_3 = 1.6$      $a_7 = 1.5714$

$a_6 = 1.625$      $a_8 = 1.5625$

B)  $a_n = \frac{6n^2 + 2n - 3}{3n^2 + 1}$

$a_1 = 1.25$      $a_5 = 2.0657$      $a_9 = 2.053$

$\lim_{n \rightarrow \infty} = 2$

$a_2 = 1.9231$      $a_4 = 2.064$      $a_{10} = 2.049$

$a_3 = 2.0357$      $a_7 = 2.060$

$a_6 = 2.0612$      $a_8 = 2.056$

2.5

C)  $a_n = \frac{5n^3 + 2n - 3}{2n^3 + 1}$

D)  $a_n = \frac{8n^4 + 2n - 3}{15n^4 + 1}$

$a_1 = 1.3$      $a_5 = 2.517$      $a_9 = 2.508$

$a_2 = 2.41$      $a_4 = 2.515$      $a_{10} = 2.507$

$a_3 = 2.509$      $a_7 = 2.512$

$a_6 = 2.519$      $a_8 = 2.510$

Find the limit of the a sequence

A)  $a_n = \frac{3n+1}{2n^2}$

$a_1 = 2$

$a_2 = .875$

$a_3 = .5$

$a_4 = .406$

$a_5 = .32$

$a_6 = .2638$

$a_7 = .2244$

$a_8 = .195$

$a_9 = .172$

$a_{10} = .155$

B)  $a_n = \frac{6n^2 + 2n - 3}{3n^5 + 1}$

C)  $a_n = \frac{10n + 2n - 3}{3n^3 + 1}$

D)  $a_n = \frac{5n^2 + 2n - 3}{10n^4 + 1}$

Find the limit of the a sequence

A)  $a_n = \frac{3n^3 + 1}{2n^2}$  DNE

$$a_1 = 2 \quad a_5 = 7.52 \quad a_9 = 13.504$$

$$a_2 = 3.125 \quad a_4 = 9.013 \quad a_{10} = 15.005$$

$$a_3 = 4.5 \quad a_7 = 16.51$$

$$a_6 = 6.03 \quad a_8 = 12.008$$

B)  $a_n = \frac{6n^4 + 2n - 3}{3n^2 + 1}$

C)  $a_n = \frac{6n^5 + 1}{3n^2}$

D)  $a_n = \frac{6n^4 - 5n^3 + 1}{3n^3 + 2n + 1}$

Find the limit of the sequence

A)  $a_n = \left( \frac{1}{n} - 4 \right) \left( \frac{3}{n} - 1 \right)$

B)  $a_n = \left( \frac{3n^3 + 4n + 2}{n^2 + 1} \right) \left( \frac{5n^2 - 32}{2n^4 + 7} \right)$

